Overview of Storage and Indexing

(Chapter 9, 3rd edition)

"How index-learning turns no student pale Yet holds the eel of science by the tail." -- Alexander Pope (1688-1744)

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Data on External Storage

<u>Disks:</u> Can retrieve random page at fixed cost - But reading several consecutive pages is much cheaper than reading them in random order

Tapes: Can only read pages in sequence

- Way Cheaper than disks; used for archival storage File organization: Method of arranging a file of records on external storage.

- Record id (rid) is sufficient to physically locate record
- Indexes are data structures that allow us to find the record ids of records with given values in index search key fields

<u>Architecture:</u> Buffer manager stages pages from external storage to main memory buffer pool. File and index layers make calls to the buffer manager.

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Alternative File Types

Many alternatives exist, *each ideal for some situations, and not so good for others:*

- <u>Heap (random order) files:</u> pages that are linked and recordes are in MO particular order
- <u>Sorted Files:</u> contiguous pages on the disk is used and records are sorted. Can apply "divide and conquer"
- <u>Clustered Files:</u> Pages that are linked and records are stored in sorted order, but NOT with contiguous pages
- Indexes: Data structures to organize records via trees or hashing.

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Impact of Alternative File Organizations

Many alternatives exist, *each ideal for some situations, and not so good for others:*

- <u>Heap (random order) files:</u> Suitable when typical access is a file scan retrieving all records.
- <u>Sorted Files</u>: Best if records must be retrieved in some order, or only a `range' of records is needed. Binary search can be applied
- <u>Clustered Files</u>: suited for range search with index. Binary search cannot be applied

- Indexes:

Like sorted/clustered files, they speed up searches for a subset of records, based on values in certain ("search key") fields

Updates are much faster than in sorted files. Why?

Indexes

An *index* on a file speeds up selections on the *search key fields* for the index.

- Any subset of the fields of a relation can be the search key for an index on the relation.
- *Search key (search field or search attribute)* is not the same as a *key* (minimal set of fields that uniquely identify a record in a relation).

An index contains a collection of *data entries*, and supports efficient retrieval of all data entries \mathbf{k}^* with a given key value \mathbf{k} .

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*Alternatives for Data Entry k** *in Index*

Three alternatives:

- Data record with key value k
- <k, rid of data record with search key value k>
- <k, list of rids of data records with search key k>

Choice of alternative for data entries is orthogonal to the indexing technique used to locate data entries with a given key value **k**.

- Examples of indexing techniques: B+ trees, hashbased structures
- Typically, index contains auxiliary information that directs searches to the desired data entries

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Alternatives for Data Entries (Contd.)

Alternative 1:

- If this is used, index structure is a file organization for data records (instead of a Heap file or sorted file).
- At most one index on a given collection of data records can use Alternative 1. (Otherwise, data records are duplicated, leading to redundant storage and potential inconsistency.)
- If data records are very large, # of pages containing data entries is high. Implies size of auxiliary information in the index is also large, typically.

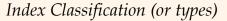
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Alternatives for Data Entries (Contd.)

Alternatives 2 (widely used) and 3:

- Key entries are typically **much smaller** than data records. So, better than Alternative 1 with large data records, especially if search keys are small. (Portion of index structure used to direct search, which depends on size of data entries, is much smaller than with Alternative 1.)
- Alternative 3 is more compact than Alternative 2, but leads to variable sized data entries even if search keys are of fixed length.

Under what conditions do we need alternative 3?



Primary vs. *secondary*: If search key contains primary key, then called primary index.

- Unique index: Search key contains a candidate key. Alt 2 is fine! (why?)

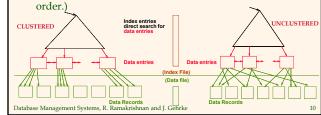
Clustered vs. *unclustered*: If order of data records is the same as, or `close to', order of data (or key) entries, then called clustered index.

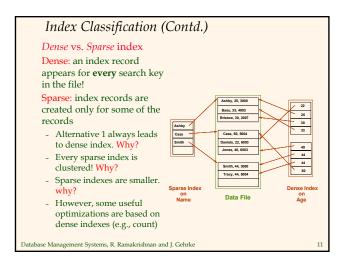
- Alternative 1 implies clustered; in practice, clustered also implies Alternative 1 (since sorted files are rare).
- A file can be clustered (or sorted) on at most one search key.
- Cost of retrieving data records through index varies *greatly* based on whether index is clustered or not!
- If there are multiple indexes, only one can be clustered! Why?
- Need to be chosen judiciously.

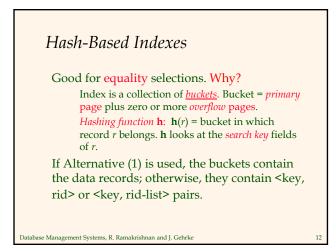
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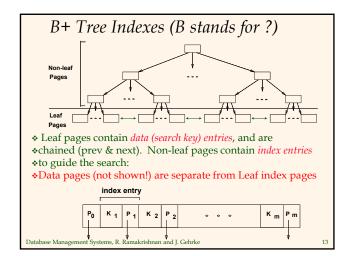
Clustered vs. Unclustered Index Suppose that Alternative (2) is used for data entries, and that the data records are stored in a Heap file. - To build clustered index, first sort the Heap file (with some free space on each page for future inserts).

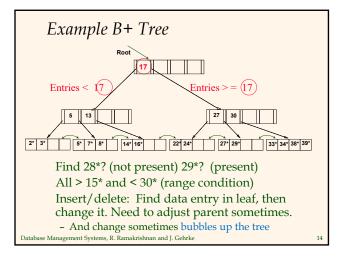
Overflow pages may be needed for inserts. (Thus, order of data recs is 'close to', but may not be identical to, the sort and a)

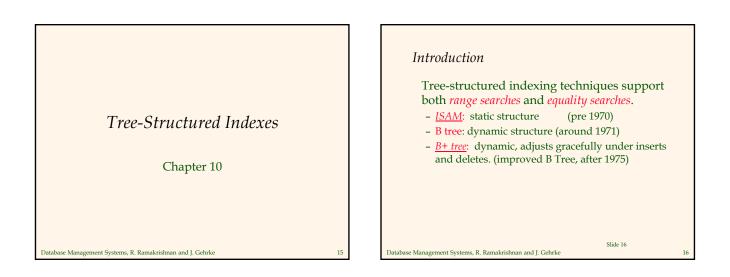


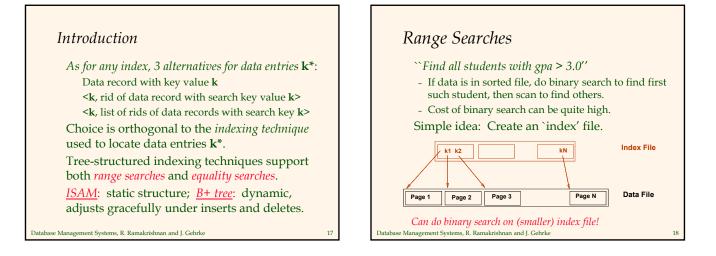












Example	(sorted	vs.	tree	indexing)	
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10000 pages sorted (contiguous) Search on the data pages takes log₂10000 or 14 page accesses (log ₂10000 is 14 + 1 more for data access)

Let the record size be 200 bytes; key size be 10 bytes, 40 records/page (8K page size)

Now the data pages and leaf nodes of the index for the above are as follows:

- 10000*40 = 400000 keys
- Key, ptr pairs per page is 8000/20 = 400
 (10 bytes for pointer and 10 bytes for the key
- (10 bytes for pointer and 10 bytes for the key)
 Fan out of the index tree is ~ 400
- # of index leaf pages is 400000/400 (key, ptr per page)= 1000 pages

We reduce page access from 14+1 to 2+1 (why?) with the index

Log₄₀₀ 1000 is 2 (+ 1 more access for the data)

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Indexes

Binary Trees

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AVL Trees ISAM (used by DBMSs before B and B+ trees) B Trees (height Balanced) B+ trees (also height balanced)

Index Characteristics

Static Vs. Dynamic Top Down Vs. Bottom up Fixed number Vs. dynamic number of index pages Balanced Vs. Unbalanced

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Binary and AVL trees

Binary trees

- At most 2 descendents (or children) per node.
- No constraint on the length of the paths from the root.

AVL trees

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 An AVL tree is a binary tree in which the difference between the height of the right and left sub-trees (or the root node) is never more than one.

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Binary and Avl trees

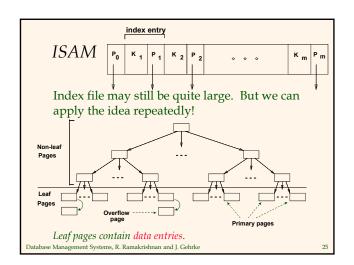
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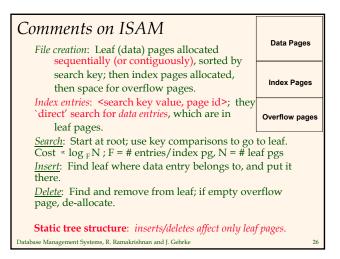
Binary and AVL are top-down tree constructions. Once the wrong key is placed in the root of the tree (or in the root of any sub tree), it is difficult to balance the tree without significant overhead (reorganization)

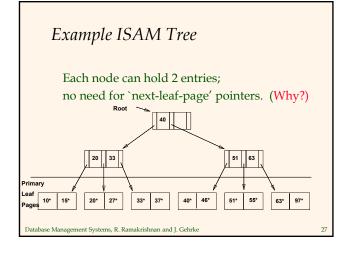
How can we guarantee that each of the pages contain at least some minimum number of keys (important for large page sizes)

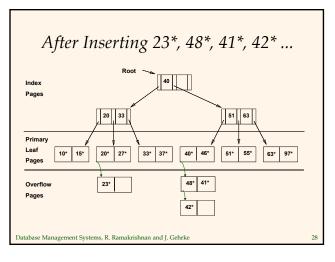
How can we guarantee that the heights of different paths are the same (or are not very different)

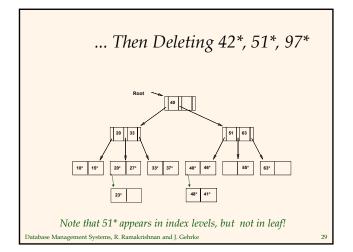
Balanced (B and B+) trees
A balanced tree builds the tree upward from the bottom instead of downward (like AVL and binary trees) from the top.
Rather than finding ways to undo a bad situation, the problem is avoided altogether from the very beginning.
With balanced trees, you allow the root to split and merge, rather than set it up and find ways to change it.











Summary of ISAM

ISAM structure is created for a given file Number of index pages (entries) do not change Overflow pages are added and deleted as needed The number of **primary** leaf pages do not change Leaf pages are allocated sequentially (hence no need for pointers!) No need to lock index pages (more concurrency) why? The index tree is NOT balanced dynamically (balanced statically at creation time) Index value exists, but may not be a record for that value Potentially long overflow lists May need to re-create ISAM index to overcome the above Database Management Systems, R. Ramakrishnan and J. Gehrke

B and *B*+ trees

The common theme of all index structures is that they associatively map some attribute of a data object to some locator information which can be used to retrieve the actual data object.

Typically, index scans are separated from record lookup:

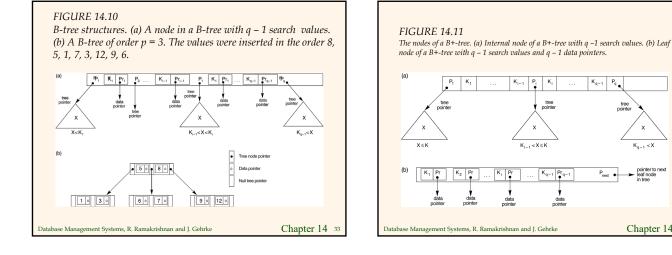
- Allows to scan an index without retrieving data from the data file (reduces I/O for count and other computations)
- For B+ trees, leaves (of index) can be accessed sequentially
- Joining of indices using record id (rid/tid)

B and *B*+ trees

Both are balanced trees; i.e., the length of the path from the root to any leaf node is the same. Both store pointers to data (in Alt 2 and 3) in the index nodes. Alt 1 is typically not used!! The data records are stored on separate pages. Both are constructed in a bottom-up manner However, there are some fundamental differences between them

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B-*Tree*

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B tree index nodes/pages (both leaf and nonleaf) contain <key, data ptr, child ptr> whereas a B+ tree non-leaf index node/ page contains <key, child ptr> pairs and B+ tree index leaf node/page contains <key, data ptr> pairs B+ tree leaf index pages/nodes are doubly linked Data pages are separate in both the cases

B Tree -- Implications

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- In a B tree (as compared to a B+ tree):
- Packing density of an index page is less (why?)

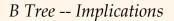
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tree

pointer to next leaf node

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- Key values are NOT repeated in the index (why?)
- Leaf index pages cannot be traversed for scan (why?)
- For a key that exists in the file, search may be stopped before reaching the leaf node (why?)



Sequential access of the entire file requires touching every node in the index (why?) - What kind of traversal is needed?

Perhaps good (why?) when the key forms most of the data record.

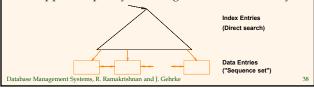
- i.e., the ratio of data record size to key size is closer to 1!

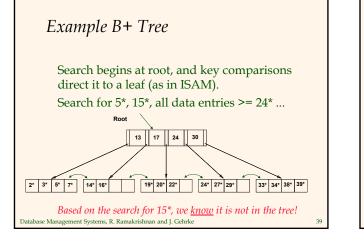
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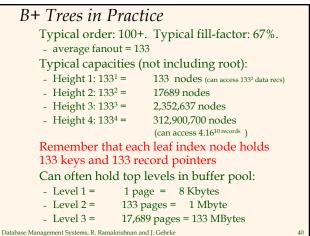
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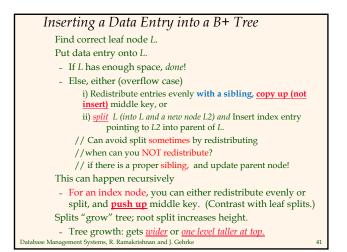
B+ Tree: Most Widely Used Index

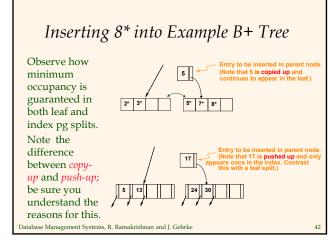
Insert/delete at $\log_F N \cosh$; keep tree *height-balanced*. (F = fanout, N = # leaf pages) Minimum 50% occupancy (except for root). Each node contains $d \le \underline{m} \le 2d$ entries. The parameter **d** is called the *order* of the tree. Supports equality and range-searches efficiently.

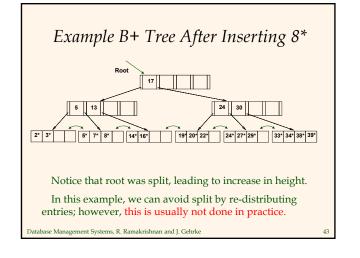


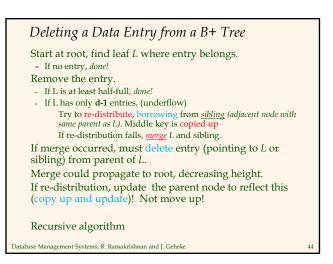


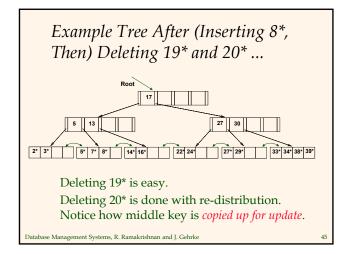


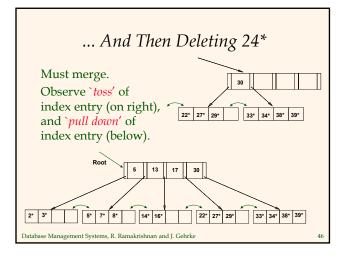


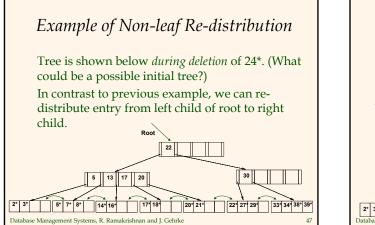


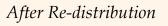




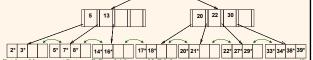








Intuitively, entries are **re-distributed by** `*pushing through*' the splitting entry in the parent node. It suffices to re-distribute index entry with key 20; we've re-distributed 17 as well for illustration.



Prefix Key Compression

Important to increase fan-out. (Why?) Key values in index entries only `direct traffic'; can often compress them.

- E.g., If we have adjacent index entries with search key values Dannon Yogurt, David Smith and Devarakonda Murthy, we can abbreviate David Smith to Dav. (The other keys can be compressed too.))
- compressed too ...) Is this correct? Not quite! What if there is a data entry *Davey Jones*? (Can only compress *David Smith* to *Davi*)

In general, while compressing, must leave each index entry greater than every key value (in any subtree) to its left. Insert/delete must be suitably modified.

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Bulk Loading of a B+ Tree

If we have a large collection of records, and we want to create a B+ tree on some field, doing so by repeatedly inserting records is very slow. <u>Bulk Loading</u> can be done much more efficiently. *Initialization*: Sort all data entries, insert pointer to first (leaf index) page in a new (root) page.



Bulk Loading (Contd.)
Root 10 20 Index entries for leaf
entered into right- most index page just
When this fills up, it splits. (Split may go up right-most path
to the root.) Much faster than
repeated inserts, especially when one considers locking! Database Management Systems, R Basia this has an unit in 121 13 20122 23131 23596 381411 444 51

Cost of bulk loading (creating an index)

- 1) Creating the data entries to insert in the index
- 2) Sort the data entries
- 3) Building the index
- Cost of 1) is (R+E), R #pages containing records and E is the # of pages with data entries; access each page of R to get the data entries Sort cost: approximately 4E Cost of writing out all the index pages

Summary of Bulk Loading

Option 1: multiple inserts.

- Slow.

- Does not give sequential storage of leaves.

Option 2: Bulk Loading

- Has advantages for concurrency control.
- Fewer I/Os during build.
- Leaves will be stored sequentially (and linked, of course).
- Can control "fill factor" on pages.

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A Note on `Order'

Order (**d**) concept replaced by physical space criterion in practice (*`at least half-full'*).

- Index pages can typically hold many more entries than leaf pages.
- Variable sized records and search keys mean different nodes will contain different numbers of entries.
- Even with fixed length fields, multiple records with the same search key value (*duplicates*) can lead to variable-sized data entries (if we use Alternative (3)).

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A Note on Alt 3

Storing multiple data pointers is not desirable as it gives rise to variable size records in leaf index pages!

For clustered B+ tree index, this can be done relatively easily by scanning additional data records on the same page as it is clustered on key value

For non-clustered B+ tree index, the above cannot be done. (why?)

 One possibility is to add overflow pages from the leaf index page that points to multiple data records!

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Summary B and B+ trees can be viewed as multi-level indexes or height balanced trees. B and B+ trees overcome the problems associated

B and B+ trees overcome the problems associated with binary and AVL trees

- Binary requires too many i/os (log 2)
- May be expensive to keep the index sorted
- Very sensitive to order of inserts
- Avl is a height balanced 1-tree or HB(1) tree

B and B+ trees are height-balanced 0-tree or H(0) or completely balanced

Summary

Tree-structured indexes are ideal for rangesearches, also good for equality searches. ISAM is a static structure.

- Only leaf pages modified; overflow pages needed.
- Overflow chains can degrade performance unless size of data set and data distribution stay constant.
- B+ tree is a dynamic structure.
- Inserts/deletes leave tree height-balanced; log $_{\rm F}$ N cost.
- High fanout (F) means depth rarely more than 3 or 4.
- Almost always better than maintaining a sorted file.

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Summary (Contd.)

- Typically, 67% occupancy on average.
- Usually preferable to ISAM, modulo *locking* considerations; adjusts to growth gracefully.
- If data entries are data records, splits can change rids!
- Key compression increases fanout, reduces height.
- Bulk loading can be much faster than repeated inserts for creating a B+ tree on a large data set.
- Most widely used index in database management systems because of its versatility. One of the most optimized components of a DBMS.

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